### INSTRUCTIONS

You may work in pairs and fiel YDOLOOGY school.

We will supply each team member MEDIAATraphing Calculator. Please leave your personal calculators at the front of the room.

Work as many of the problems as you can in the time allotted. You should not expect to finish every problem, so choose the ones you can readily complete.

The number of points earned will det DMCSD inners. Be aware there is NO penalty for quessing.

LOOHOR HOHOR HOHOR

The judges must score som YAG GUIII HAM. In this case, one team member will take the calculator to the appropriate judge for immediate grading. The judge will note the score for that question and will add it to your team score after the competition is over.

order to improve this event for next year's competition, we would appreciate your feedback. Thanks for participating the participating of the participating

You may keep this test to prepare for next year's Technology Tandem competition, as the contents of the event may be similar to this year's event.

Each answer is worth five points.

Sponsored by: CUYAMACA COMMUNITY COLLEGE

#### INSTRUCTIONS:

You may work in pairs and field a maximum of two teams per school.

We will supply each team member with a TI-84 Graphing Calculator. Please leave your personal calculators at the front of the room.

Work as many of the problems as you can in the time allotted. You should not expect to finish every problem, so choose the ones you can readily complete.

The number of points earned will determine the winners. Be aware there is **NO penalty for guessing**.

The judges must score some of the problems on the spot. In this case, one team member will take the calculator to the appropriate judge for immediate grading. The judge will note the score for that question and will add it to your team score after the competition is over.

In order to improve this event for next year's competition, we would appreciate your feedback. Thanks for participating!

You may keep this test to prepare for next year's Technology Tandem competition, as the contents of the event may be similar to this year's event.

Each answer is worth five points.

Sponsored by: CUYAMACA COMMUNITY COLLEGE

- 1. Find the prime factorization of 43358976. Find the prime factorization of 43358976.
- 2. Find the prime factorization of 2736832813.
- 3. Find the prime factorization of 90874860.
- 4. Find the smallest pair of twin primes greater than 40.
- 5. Find the smallest pair of twin primes greater than 2007.
- 6. Find the next pair of twin primes greater than 2007 (i.e. the first pair greater than the pair found in the previous problem).
- 7. Find the first pair of twin primes greater than one million.
- .76307 fo noits zirotos aming and bni 3.8 many times does  $y = 20\cos(200x)$  take on the value 15 on the interval
- 9. Find a pair of twin primes between 8000 and 8100.
- 10. Find the greatest common factor of 384870629 and 1110439.
- 11. Find the least common multiple of 3145149 and 22818509.
- ? such that the sum of the sum o

13. Solve 
$$\sqrt{\frac{-(x+1)! + (x+2)! + (x-3)! - x!}{\frac{(x-4)!(x-1)!}{x! + 3 \cdot 5 \cdot 7}} + 8002 - 36163 = 2007}$$
14. Solve 
$$\left(x^3 - 6x^2 - 10x - 2039\right)^{\frac{x^2 - 18x - 24}{\sqrt{x^4 - 3x^3 + 13x^2 + 7x + 756}}} = 191$$

14. Solve 
$$(x^3 - 6x^2 - 10x - 2039)^{\frac{x^2 - 18x - 24}{\sqrt{x^4 - 3x^3 + 13x^2 + 7x + 756}}} = 191$$
.

- 15. Let k be the least positive integer that is divisible by each of the first ten natural numbers. Find  $\left(\frac{k}{5005} + 144\right)^{\frac{1}{6}}$
- 16. What is the exact sum of all the intercepts of the graph of then the pair found in the previous problem).
- Find the exact value of  $\sum_{k=1}^{k} \frac{k}{4^k}$ .
- 18. How many times does  $y = 20\cos(200x)$  take on the value 15 on the interval Find the prime factorization of 70637.

$$\sqrt{2\sqrt{2\sqrt{2}}} = \frac{1}{110439} = \frac{1}$$

- 20. How many pairs of integers (a, b) are there for which  $a^2 b^2 = 256$ .
- 21. Create a graph in polar coordinates of a flower with ten petals where each petal is 3 units long and a tip of a petal intersects with each axis. Show the graph to an instructor and be sure to set the graphing window and axes scales so that the instructor can readily see the lengths of the petals, the number of petals, and their placement with regard to the axes (bring your

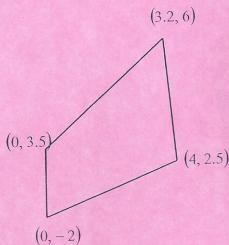
## 25. Find the area of the region defined be the vertices given: EdDNAINE AITO ABNA shape is not drawn to scale).

The area of a triangle with vertices  $(x_1, y_1)$ ,  $(x_2, y_2)$ , and  $(x_3, y_3)$  can be determined by evaluating the following determinant:

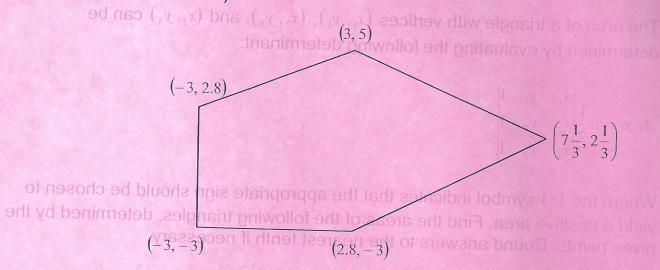
$$Area = \pm \frac{1}{2} \begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix}$$

Where the  $(\pm)$  symbol indicates that the appropriate sign should be chosen to yield a positive area. Find the areas of the following triangles, determined by the given points. Round answers to the nearest tenth if necessary.

- 22. Triangle's vertices: (1, 3), (2, 7), and (8, 4).
- and all values of  $\psi$  for which the triangle with the following vertices has an 23. Triangle's vertices: (-5,4),  $(e^2,4)$ , and  $(6,-\sqrt{37})$ .
- 24. Find the area of the region defined be the vertices given below (note: the shape is not drawn to scale).

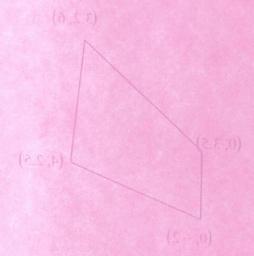


25. Find the area of the region defined be the vertices given below (note: the shape is not drawn to scale).



26. Find all values of y for which the triangle with the following vertices has an area of 100: (-1,5), (-6,-2), (4,y).

nd the area of the region defined be the vertices given below (note: the



# # 32 – 35) in a seven-year study of ten of the nation's most selective colleges and: SOITSITATS in the selective, researchers found that a student applicant has a better chance of being accepted.

Without using the variance and standard deviation functions of your graphing calculator, we'll find the variance and standard deviation for the following data observations.

	Regular									
3.8	39 2.23	2.	58	2.07	2.94	2.29	3.14	2.15	1.95	0.51
2.8	36 1.48	1.	12	2.76	3.10	1.05	2.23	1.70	5.57	2.81
7.2	24 3.29	1.	87	3.48	2.99	3.48	2.12	4.69	2.29	2.02
	CT			60						

- 27. Create a list, L1, of these data, and use the list to find the mean,  $\bar{x}$ , for these data (do not round your result).

  A but I and I are some fine and I are so
- 28. Create a second list, L2, of the deviations from the mean; i.e. calculate  $x \bar{x}$ , for each observation, x, in L1 and store these deviations in L2. Sum L2. (Do not round your result). Store and to the deviation of the second store these deviations in L2. Sum the second of the second store that the second store the second store the second store that the second st
- 29. Create a third list, L3, of the squares of the deviations in L2; i.e. calculate  $(x \bar{x})^2$  for each observation, x. To find the variance for the original data observations, find the arithmetic mean of the entries in L3. Note: our variance may differ from applying the graphing calculator's variance function to the original data observations. (Do not round your result).
- 30. The standard deviation, sd, for the original data observations is the square root of the variance found in the previous problem. Find the standard deviation, sd (round to the nearest thousandth if necessary).
- 31. The z-score (or standard score) for any given observation, x, is  $\frac{x-x}{sd}$ . Create a fourth list, L4, of the z-scores for the original data observations. What is the maximum z-score in the list (rounded to the nearest thousandth, if necessary).

(# 32 – 35) In a seven-year study of ten of the nation's most selective colleges and universities, researchers found that a student applicant has a better chance of being accepted to a college through early decision rather than by regular decision. The table below shows a comparison of SAT scores (out of 1600) and acceptance rates by both systems.

Let E(s) and R(s) be the percentages of early decision and regular decision applicants, respectively, which were accepted.

SAT Score	% Accepted Early	% Accepted Regular		
1145	- 21	10		
1245	35	17		
1345	52	31		
8 1445 00	8470 78	48		
1550	93	72		

- Create a list, L1, of these data, and use the list to find the mean, x, for these
- 32. Find the regression equations for E and R. (For each model be sure to determine which would be the best fit –either linear or exponential). Round the constants to 4 decimal places.
- 33. For early decision applicants who score 1425 points, what percentage get accepted? What about for regular decision applicants who score 1425 points? (Round to the nearest hundredth).
- 34. For what score do half of early decision applicants get accepted? What about for regular decision applicants? (Round to the nearest whole number).
- 35. Use your graphing calculator to find the intersection point(s) of the graphs of E and R. What does this point(s) represent in terms of the situation?

he standard deviation, *sd*, for the original data observations is the square out of the variance found in the previous problem. Find the standard eviation, *sd* (round to the nearest thousandth if necessary).

ente a fourth list. L4, of the z-scores for the original data observations.

Solve the following system of equations (write rational solu:20POTrARBEDJA notation, and round irrational solutions to the nearest tenth).

Unless you are directed to do otherwise, round irrational numbers to the nearest hundredth. Do not round rational numbers.

36. Use your calculator to find the equation of the quadratic function that passes through the following points (do not round):

Solve the following system of equations (write 2,01) bns, (4.75,21,21) and round inational solutions to the nearest tenth)

37. Use your calculator to find the equation of the cubic function that passes through the following points (do not round):

(-5, -423.0973), (-2, 4.15514), (5, 471.1173), and (10, 3757.2971)

ve the quadratic inequality, and write your solution (if it exists) in interval ation (round to the nearest tenth if necessary)

38. Use your calculator to find the equation of the logarithmic function that passes through the following points:

 $(e^{-3}, 12.46), (e^{2}, 0.06), (e^{5}, -7.38)$ 

e inequality, and write your solution (if it exists) in interval notation the nearest tenth if necessary)

39. Use your calculator to find the equation of the exponential function passing through the points:

(2, -38.33), (4, -524.76508)

40. Solve the following system of equations (round to the nearest hundredth).

3.2x - 5.7y = 4

-2.4x + 3.8y = 7

41. Solve the following system of equations (write rational solutions in fractional notation, and round irrational solutions to the nearest tenth).

Unless you are directed to do otherwise, round irrational numbers to the nearest numbers. 
$$z = x + y + z = x + z$$

42. Solve the following system of equations (write rational solutions in fractional notation, and round irrational solutions to the nearest tenth).

Use your calculator to find the equation of the cubic function that passes 
$$2x + z = 5$$
  $2x + z = 5$ 

$$7x - z = 1$$

43. Solve the quadratic inequality, and write your solution (if it exists) in interval notation (round to the nearest tenth if necessary).

$$-.5x^2 - 2.4x + 18.6 < 9.76$$

44. Solve the inequality, and write your solution (if it exists) in interval notation (round to the nearest tenth if necessary).

phisseq noithnut laitnenouse and to not supplied to not supplied to the nearest tenth if necessary).

$$x^4 - 2x^3 - 38.23x^2 + 23.63x + 144.2376 \ge 0$$

$$(x-4)^2 + (y+1)^2 = 256$$

$$(x-5)^2 - (y-2)^2 = 121$$

46. Solve the following equation (if necessary, round to the nearest hundredth).

A chyptogram is a message written according to a secret code. Matrix multiplication can be used to encode \$18773.8 + \$28676.0 \( \frac{9}{2} \) \( \frac{5}{2} \) \( \frac{5}

47. Factor the following polynomial completely (use only integers – no fractions and no rounding).

and notified bluow ew next wints a SXS as a xintern priboone nuo it elements as  $x^2 + 5x^2 - 87x^4 + 43x^3 + 902x^2 - 672x - 1440$  and  $x^2 + 5x^2 - 87x^4 + 43x^3 + 902x^2 - 672x - 1440$  and  $x^2 + 5x^2 - 87x^4 + 43x^3 + 902x^2 - 672x - 1440$ 

Use the matrices defined below for the following four problems. Do not use decimal notation in your matrix entries. Use fraction notation for rational numbers (excluding integers).

 $A = \begin{bmatrix} -2 & 1 & 4 \\ 2 & 3 & 0 & -4 \\ 1 & 1 & 7 \end{bmatrix}^{2} = \begin{bmatrix} 0 & 1 & 3 & 2 \\ 5 & -4 & 1 & 6 \\ 2 & -3 & 8 \end{bmatrix}$  where  $B = \begin{bmatrix} -2 & 1 & 4 \\ 5 & 1 & 6 \\ 2 & -3 & 8 \end{bmatrix}$  and  $B = \begin{bmatrix} -2 & 1 & 4 \\ 5 & 1 & 6 \\ 2 & -3 & 8 \end{bmatrix}$ 

- 48. Find AB.
- 49. If  $f(x) = 2x^4 + x^3 8x^2$ , evaluate f(B).

encode the following message

50. Find the multiplicative inverse of matrix A (remember to use fractions – not decimals).

### Solve the following equation (if necessary, round to the nearest hundredth).

A cryptogram is a message written according to a secret code. Matrix multiplication can be used to encode and decode messages. First we assign a number to each letter of the alphabet (A = 1, B = 2, C = 3, ..., Z = 26) and assign the number 0 to a blank space. Then any message is converted to numbers and partitioned into uncoded row matrices, each with the appropriate number of entries.

For example, if our encoding matrix is a 3X3 matrix, then we would partition the message "MEET ME MONDAY" into the following 1X3 row matrices.

To encode the message we might use the matrix 
$$A = \begin{bmatrix} -1 & 0 & 2 \\ 3 & 1 & -4 \\ -2 & -3 & 5 \end{bmatrix}$$
 as follows Uncoded Encoding Coded

Uncoded Encoding Coded Message Matrix A Message 
$$\begin{bmatrix} -1 & 0 & 2 \\ 3 & 1 & -4 \\ -2 & -3 & 5 \end{bmatrix} = \begin{bmatrix} -8 & -10 & 31 \end{bmatrix}$$

51. Given the encoding matrix 
$$A = \begin{bmatrix} -2 & 1 & 4 \\ 3 & 0 & -4 \\ 1 & 1 & 7 \end{bmatrix}$$
, encode the following message.

CAPTAIN OLIVER LOVES TO DRIVE

52. Given that the encoding matrix 
$$B = \begin{bmatrix} 5 & 3 & 2 \\ -4 & 1 & 6 \\ 2 & -3 & 8 \end{bmatrix}$$
 was used to create the following coded message, decode the message.

53. Draw a skate-boarder moving across your graphing window. Show it to one of the instructors (bring your answer sheet with you).

END